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## Confirmation of paper submission

Berlin, 28. April 2014

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**Title of Paper:** Numerical Simulations of Re-ignition of Quenched  
Detonation Waves behind a Backward-facing Step  
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# Numerical Simulations of Re-ignition of Quenched Detonation Waves behind a Backward-facing Step



## Abstract.

Re-ignition and re-initiation mechanisms of quenched detonation waves passing over a backward facing step are studied numerically using a high-order Discontinuous Galerkin method with detailed thermo.chemistry. A stoichiometric Hydrogen/Oxygen mixture with different diluents (Argon and Nitrogen) is considered to assess effects of mixture composition and re-activity on the initiation process. It is found that the wall reflection of the decoupled shock plays a critical role in controlling the formation and growth of the ignition kernels and the possible transition to detonation. Through parametric studies, it is shown that for more reactive Argon-diluted mixtures, ignition appears first behind the regular shock reflection, which is followed by spontaneous re-initiation. By replacing Argon with Nitrogen, the reactivity reduces and re-ignition through Mach reflection is observed. This ignition phenomenon is affected by the adiabatic heating behind the Mach stem and the enhanced mixing along the slip-line due to hydrodynamic instabilities. The present numerical investigation shows good agreement with corresponding experimental measurements and confirms previous postulations regarding the role of the Mach reflection on the re-ignition.

## Introduction.

Detonation is a highly energetic combustion process, involving a compression shock and an attached flame, which provides fast heat release as a driving source. The formation and the quenching of these detonation waves exhibits a pronounced sensitivity to the geometry. For example, with abruptly expanding geometries, the detonation wave can be significantly delayed or potentially quenched. The reason for this phenomenon is as follows. As the shock gradually weakens during the expansion, the post-shock state becomes less favorable for highly sensitive chemical reactions. Thus, the flame gradually decouples from the shock front, which results in the breakdown of the positive feedback. However, since the detached shock is also capable of interacting with downstream geometric boundaries, it has been found that the delay or quenched detonation front can be re-ignited under certain conditions. The investigation and analysis of the re-ignition has significance for practical applications. In fact, the process described above is analogous to those encountered in many detonation facilities. In pulse detonation engines, for example, detonation, after being initiated in the initiator section, passes over an expanding nozzle and propagates into the larger combustion chamber. Furthermore, it is also related to the deflagration-to-detonation transition (DDT) in obstructed tubes with periodically arranged obstacles. As such, the further understanding of these processes not only deepens our understanding of detonation physics, but will also provide further guidance for practical designs. Although notable progress has been made on identifying re-ignition mechanisms of quenched detonation waves, conclusions from different studies are sometimes inconsistent and disputable. With interest to the present investigation, the following re-ignition processes are summarized: 1) Autoignition and re-initiation by regular shock reflection: The autoignition of a quenched detonation wave is induced by a regular reflection of the flame-detached shock-wave. Lee pointed out that this mode exhibits similarities to the triple-point collision in multi-dimensional detonation systems. Fast autoignition will re-initiate the detonation with a strongly overdriven explosion. The onset and dynamics of this re-ignition mode have been indirectly deduced from experimental soot-

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foilrecords, and observed from numerical simulations using one-step chemical mechanisms.2) Autoignition and re-initiation by Mach reflection: When the incident shock angle exceeds a critical value, Mach reflection can occur. This results in the formation of a high-temperature region behind the Mach stem, which promotes ignition and re-initiation. This mechanism was deduced from experimental investigations of detonation waves passing over a backward-facing step. Even in subsequent experiments, however, the distinction to ignition by regular reflection could not be isolated due to the limited spatio-temporal resolution of the measurement method. Ignition by Mach-heating was also emphasized in a computational study on DDT in channels with periodically positioned obstacles. These simulations showed that by varying the spacing between obstacles to promote Mach reflection, the heating of the fresh mixture by the collision of the strong Mach stem with the downstream obstacle leads to the onset of detonation. Ignition by Mach heating was also observed in complex wave interactions. However, by excluding these confinement effects and geometric interactions, it remains unclear whether and how transitions to detonation is facilitated.3) Re-initiation by hydrodynamic instabilities: This mechanism, first postulated by Teodorczyk et al., emphasizes the effect of enhanced mixing between reaction products and unburned gases by Kelvin-Helmholtz (KH) or Richtmyer-Meshkov (RM) instabilities. This is similar to the ignition mechanism proposed by Radulescu et al. in irregular detonation waves. Recently, a more detailed study has been conducted by Bhattacharjee et al., who studied the re-ignition process of a quenched detonation behind a circular obstacle. At certain conditions, they found that the occurrence of a rapidly burning mixture is strongly coupled to the presence of a wall jet, which enhances the mixing and growth of the flame front behind the Mach stem. As postulated, this might lead to the onset of transverse detonation waves. However, the transition to detonation from hot-spot ignition appears non-deterministic under these operating conditions since the re-initiation could not be systematically reproduced. The objective of this work is to provide a better characterization of re-ignition events of quenched detonation waves. Since the shock reflection plays an important role, an analytic model will first be proposed to analyze shock reflection based on quasi-steady assumptions. This low-order model allows us to evaluate the thermodynamic state and ignition delay of the shock-compressed mixture. These theoretical investigations are complemented by detailed simulations using a high-order Discontinuous Galerkin approach. A detailed chemical kinetics model is employed to provide an accurate representation of rate-controlling quenching and ignition events. The geometric configuration under consideration is identical to the experiment by Ohyagi et al. After identifying and discussing relevant physics, the simulation results will then be used to assess the validity of the reduced-order model.

### **Approach.**

In this work, the 2D reactive Euler equations are solved using a discontinuous Galerkin (DG) method. For this, the computational domain is subdivided into a set of elements. For this, several algorithmic aspects require consideration to enable the application to chemically reacting flows. First, the variable thermodynamic properties, specifically the temperature- and composition-dependent heat capacities introduce spurious oscillations for fully conservative flux formulations. To prevent these oscillations, a relaxation method is applied, leading to a framework with quasi-conservation of energy. Second, the detailed chemistry representation introduces a

chemically sti. system. A splitting scheme is used for the temporal integration, in which the convection operator is handled explicitly and the reaction source term is advanced implicitly. Finally, the consideration of discontinuities due to shocks and contact interfaces is treated using a WENO-based limiter that was recently proposed by Zhong Shu. This limiter guarantees the positivity of density and pressure based on the entropy minimum principle. More details and verification of the developed computational platform can be found in the work by Lv & Ihme.

## Results and discussion.

In this study, we consider the experimental configuration of Ohyagi et al. In this facility, a long initiator section is adopted to ensure fully-developed cellular structures before the detonation wave expands into the combustion section. The height of the combustor section is three times the cross-section of the initiator. All simulations were initialized with a 1D Chapman-Jouguet (CJ) wave near the inlet of the initiator section. Small perturbations were imposed along the shock front to initiate transition to 2D cellular structures. The detonation wave di.racts after entering the combustor section. Low initial pressure and high dilution ratios have been found to be essential in predicting the correct detonation size with detailed chemical kinetics. In the present study, the initial pressure and temperature are set to 26.7 kPa and 293 K, respectively, and the dilution ratio is fixed to 40 For all cases presented, the quenched detonation configurations are observed after the fully established detonation-wave di.racts over the backward-facing step. The decoupled shock front, propagating faster than the flame front, interacts first with the bottom wall. Under di.erent diluent parameters the shock reflection results in a di.erent ignition pattern that can lead to the successful re-initiation or the failure of the detonation. Detailed simulations are performed, showing that the di.raction induces a shock-flame complex, in which shock and flame fronts are completely decoupled. Several "finger-like" flame segments are observed behind the shock front. After the shock starts to interact with the wall, and subsequently the reflected shock transmits into the burnt mixture. After this reflection occurs, the hot spot is immediately generated around  $x = 40$  mm, followed by an extremely fast transition (on the order of few micro-seconds to an overdriven detonation, which is visible at later time. The new detonation front grows and quickly engulfs the inert transverse wave. After it catches up with the leading incident shock, a reactive Mach stem is formed due to their mutual interactions. The induced hydrodynamic instabilities along the slip line is well resolved in our simulation. The forward wall jetting e.ect behind the Mach stem is also observed. The new triple point, connecting the reactive Mach stem, reactive transverse wave and inert incident shock, moves along the curved front of the incident shock, and finally re-initiates the whole front. This re-initiation sequence shows very good agreement with that reported in the experimental study by Obara et al.

## Conclusions.

Re-ignition events of a quenched detonation wave were investigated through detailed numerical simulations using a high-order discontinuous Galerkin method. A reduced-order model was developed for the parametric investigation of the re-ignition dynamics. The quenched detonation is generated by the di.raction over a backward-facing step. A stoichiometric Hydrogen/Oxygen mixture was considered with variable diluent compositions. A series of detailed simulations was performed to systematically identify ignition mechanisms that are controlled by the coupling between gas-

dynamic processes and chemical kinetics. It was found that the shock reflection plays an essential role in the formation of ignition spots. Predictions from the reduced-order model are in qualitative agreement with the detailed simulations.

### Acknowledgements

Financial support through the NSF CAREER program with Award No. CBET-0844587 is gratefully acknowledged.

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